

# Chapter 17

## Engineering Electric Circuits: AC Electric Circuits

### 17.1 Alternating Current in a Resistor

### Homework #145

This is a copy of Homework #116 titled "Alternating Current" in "Chapter 14-DC Electric Circuits".

#### I

01. An ac voltage supply with a peak voltage of 180 V is applied across a  $480\text{-}\Omega$  resistor.

- a.) What is the value of the peak current in the resistor?
- b.) What is the value of the rms current in the resistor?

02. What is the peak current in a  $2.80\text{-k}\Omega$  resistor connected to a 240-V ac power source?

03. Determine the resistance of the following  $120\text{-V}_{\text{rms}}$  light bulbs.

- a.) 40.0 W
- b.) 60.0 W
- c.) 75.0 W
- d.) 100 W

#### II

04. What is the peak current passing through a 100-W light bulb connected to a 120-V ac line?

05. If the peak value of alternating current passing through a 1250-W electric device is 4.25 A, what is the rms voltage across it?

06. What is the maximum instantaneous value of the power dissipated by a 75.0-W light bulb?

07. A  $15.0\text{-}\Omega$  heater coil is connected to a 240-V ac line.

- a.) What is the average power used by this coil?
- b.) What is the maximum value of the instantaneous power?
- c.) What is the minimum value of the instantaneous power?

ANSWERS: **01.** a.) 0.375 A   b.) 0.265 A   **02.** 0.121 A   **03.** a.)  $360\ \Omega$    b.)  $240\ \Omega$    c.)  $192\ \Omega$    d.)  $144\ \Omega$   
**04.** 1.18 A   **05.** 416 V   **06.** 150 W   **07.** a.) 3840 W   b.) 7680 W   c.) 0 W

# Chapter 17

## Engineering Electric Circuits: AC Electric Circuits

### 17.2 Alternating Current in Inductors and Capacitors    Homework #146

**I**

01. At what frequency will a \_\_\_\_\_?  
 a.) 97.5- $\mu\text{F}$  capacitor have a reactance of 35.0  $\Omega$   
 b.) 626-mH inductor have a reactance of 1.85 k $\Omega$ ?

02. On the coordinate axes to the right, sketch a graph of reactance of a 10.0- $\mu\text{F}$  capacitor as a function of frequency from 10.0 to 1000.0 Hz. What is  $X_{\max}$  for this range?

03. On the coordinate axes to the right and below, sketch a graph of reactance of a 10.0-mH inductor as a function of frequency from 10.0 to 1000.0 Hz. What is  $X_{\max}$  for this range?

**II**

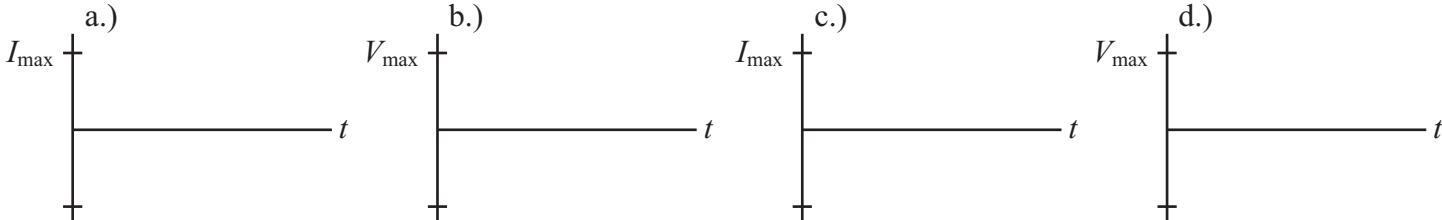
04. At what frequency would the reactance of a 10.0-mH inductor equal that of a 100.0- $\mu\text{F}$  capacitor?

05. A coil draws 2.25 A of current from a 120-V ac power supply operating at 60.0 Hz. What is the inductance of this coil?

06. A capacitor draws 2.25 A of current from a 120-V ac power supply operating at 60.0 Hz. What is the capacitance of this capacitor?

07. For each of the following circuits, use the coordinate axes below to construct the graph indicated.

- a.) A 35.0-mH inductor is wired to a 120-V ac power supply operating at 60.0 Hz. Find  $I_{\max}$  and graph  $I$  vs  $t$ .  
 b.) A 35.0-mH inductor draws 7.50 A from an ac power supply operating at 60.0 Hz. Find  $V_{\max}$  and graph  $V$  vs  $t$ .  
 c.) A 35.0- $\mu\text{F}$  capacitor is wired to a 120-V ac power supply operating at 60.0 Hz. Find  $I_{\max}$  and graph  $I$  vs  $t$ .  
 d.) A 35.0- $\mu\text{F}$  capacitor draws 7.50 A from an ac power supply operating at 60.0 Hz. Find  $V_{\max}$  and graph  $V$  vs  $t$ .

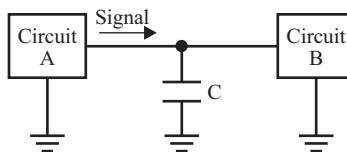


08. The diagrams below show two possible arrangements, I and II, for two circuits, A and B, and a capacitor. In both arrangements assume the capacitance of the capacitor is very large.

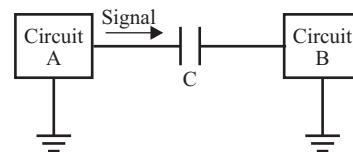
- a.) Which arrangement will allow an ac signal but not a dc signal from circuit A to B? Explain!!!  
 b.) Which arrangement will allow a dc signal but not an ac signal from circuit A to B? Explain!!!

**Problem 08**

**Arrangement I**

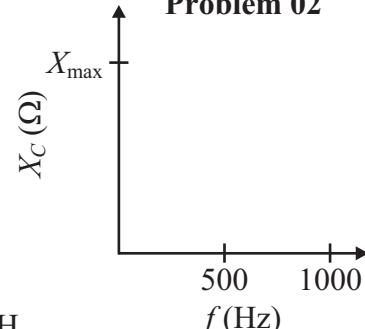


**Arrangement II**

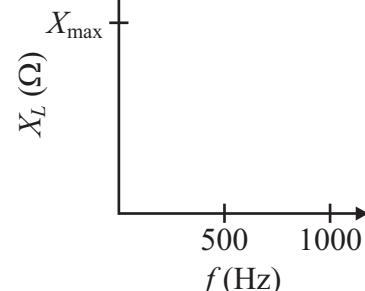


**ANSWERS:** 01. a.) 46.6 Hz   b.) 470 Hz   02. 1592  $\Omega$    03. 62.8  $\Omega$    04. 159 Hz   05. 0.141 H   06. 49.7  $\mu\text{F}$   
 07. a.) 12.9 A   b.) 140 V   c.) 2.24 A   d.) 804 V   08. a.) Arrangement II   b.) Arrangement I

**Problem 02**



**Problem 03**



# Chapter 17

## Engineering Electric Circuits: AC Electric Circuits

### 17.3 Phasors/LC and LRC Circuits Without a Generator    Homework #147

#### I

01. An LRC circuit is designed such that  $V_L > V_C$ .
- Draw the resultant phasor diagram.
  - Draw the phase angle,  $\delta$ , and indicate whether the emf of the circuit leads or lags the current by  $\delta$ .
  - Describe how the phase angle,  $\delta$ , can be calculated from  $V_R$ ,  $V_L$ , and  $V_C$ .
02. An LRC circuit is designed such that  $V_L < V_C$ .
- Draw the resultant phasor diagram.
  - Draw the phase angle,  $\delta$ , and indicate whether the emf of the circuit leads or lags the current by  $\delta$ .
  - Describe how the phase angle,  $\delta$ , can be calculated from  $V_R$ ,  $V_L$ , and  $V_C$ .
03. What is the period of oscillation of an LC circuit consisting of a 15.0-mH coil and a 150.0- $\mu\text{F}$  capacitor?
04. An LC circuit, with a 65.0- $\mu\text{F}$  capacitor, oscillates at a 60.0-Hz frequency. What is the inductance of the inductor?
05. Circuit 1 is an LC circuit that has an inductance of  $L_1$  and a capacitance of  $C_1$ . Circuit 2, a second LC circuit, has an inductance of  $L_2 = \frac{1}{2}L_1$  and a capacitance of  $C_2 = 2C_1$ , while a third LC circuit, Circuit 3, has an inductance of  $L_3 = 2L_1$  and a capacitance of  $C_3 = \frac{1}{2}C_1$ .
- Which circuit oscillates at the greatest frequency?
  - Which circuit oscillates at the least frequency?
  - If all capacitors are charged to the same voltage, which circuit would have the greatest  $I_{\max}$ ?
  - If all three circuits have the same  $I_{\max}$ , which circuit will have the inductor that has the greatest voltage?

#### II

06. A 2500 pF capacitor is charged to 60.0 V and then connected, via two wires, to a 40.0-mH inductor. The two plates of the capacitor are separated by 2.00 mm of air and each plate has an area of 0.565 m<sup>2</sup>. The length of the inductor is 10.00 cm and the coils have a radius of 1.00 cm.
- What is the total charge stored on the capacitor before it is connected to the inductor?
  - How much electric energy is stored in the capacitor before it is connected to the inductor?
  - What is the electric energy density of the capacitor before it is connected to the inductor?
  - What is the electric field strength in the capacitor before it is connected to the inductor?
  - What is the maximum magnetic energy stored in the inductor after its connection to the capacitor?
  - What is the maximum magnetic energy density of the inductor after its connection to the capacitor?
  - What is the maximum magnetic field strength in the inductor after its connection to the capacitor?
  - What is the frequency of oscillation in the circuit?
  - What is the maximum current in the circuit?
  - Write an equation that describes the charge on the capacitor as a function of time in this circuit and graph Q vs t.
  - Write an equation that describes the current in this circuit as a function of time and graph I vs t.
  - Graph Q and I as a function of time if a small resistor is connected in series with the capacitor and inductor in the circuit. (Note: The resistance of the wire that is coiled to make the inductor could serve as this resistor.)

ANSWERS: 01. b.)  $\varepsilon$  leads  $I$     c.)  $\tan \delta = \frac{V_L - V_C}{V_R}$     02. b.)  $\varepsilon$  lags  $I$     c.)  $\tan \delta = \frac{V_C - V_L}{V_R}$     03. 9.42 ms

04. 0.108 H    05. a.) none    b.) none    c.) Circuit 2    d.) Circuit 3    06. a.) 0.150  $\mu\text{C}$     b.) 4.50  $\mu\text{J}$     c.) 3.98 mJ/m<sup>3</sup>  
 06. d.)  $3.00 \times 10^4$  V/m    e.) 4.50  $\mu\text{J}$     f.) 0.143 J/m<sup>3</sup>    g.)  $6.00 \times 10^{-4}$  T    h.)  $1.59 \times 10^4$  Hz ( $\omega = 1.00 \times 10^5$  rad/s)  
 06. i.) 0.015 A    j.)  $Q = (1.50 \times 10^{-7}) \cos(1.00 \times 10^5 t)$     k.)  $I = - (0.0150) \sin(1.00 \times 10^5 t)$

# Chapter 17

## Engineering Electric Circuits: AC Electric Circuits

### 17.4 LRC Circuits With a Generator/Resonance

### Homework #148

#### I

01. An AC generator that has a maximum emf of 30.0 V and an angular frequency of 300.0 rad/s is connected in series with a 34.8- $\mu\text{F}$  capacitor and a 95.0- $\Omega$  resistor.
- What is the impedance?
  - What is the power factor?
  - What is the rms current?
  - What is the average power supplied?
02. A coil can be treated as a resistance in series with an inductor. A coil with a resistance of 80.0  $\Omega$  and an inductance of 0.350 H is connected to a 120-V, 60.0-Hz ac line.
- What is the impedance?
  - What is the power factor?
  - What is the rms current?
  - What is the average power supplied?
03. A series LCR consists of a 50.0-mH inductor, a 50.0- $\mu\text{F}$  capacitor and a 50.0- $\Omega$  resistor driven by a 50.0-V generator with a variable resistor,  $\omega$ .
- What is the resonant angular frequency  $\omega_0$ ?
  - Find  $X_L$ ,  $X_C$ ,  $Z$ ,  $I_{\text{rms}}$ , the phase angle,  $\delta$ , and the power factor at  $\omega_0$ .
  - Find  $X_L$ ,  $X_C$ ,  $Z$ ,  $I_{\text{rms}}$ , the phase angle,  $\delta$ , and the power factor when  $\omega = 3000$  rad/s.
04. FM radio stations are assigned carrier waves by the FCC in the range of 88.0 to 108.0 MHz. A radio receiver is a series LCR circuit with a variable capacitor so that it can resonate with any carrier wave frequency in this range. A particular radio has a 1.50- $\mu\text{H}$  inductor.
- What is the range of capacitances necessary to cover this range of frequencies?

**For parts b.) and c.), assume the radio is tuned to 104.6 MHz and  $\Delta f = 0.05$  MHz.**

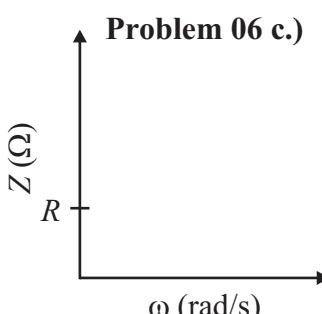
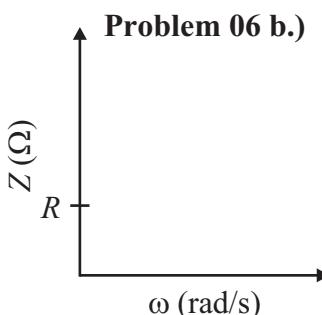
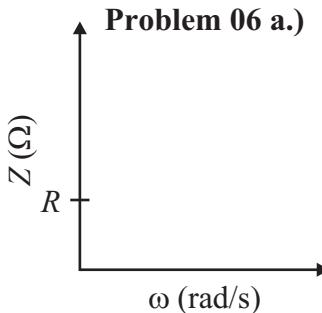
- What is the capacitance?
- What is the Q factor?

#### II

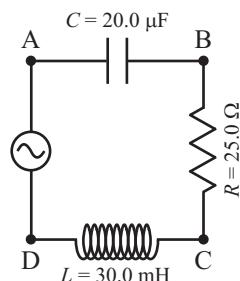
05. In the circuit shown to the right, the variable frequency ac generator produces an rms voltage of 120 V when operated at 60.0 Hz. Assume transient effects have had sufficient time to decay so steady state conditions exist.
- What is the rms current in the circuit?
  - Find the rms voltage across AB.
  - Find the rms voltage across BC.
  - Find the rms voltage across CD.
  - Find the rms voltage across AC.
  - Find the rms voltage across BD.
  - What is the maximum energy stored in the capacitor?
  - What is the maximum energy stored in the inductor?
  - What is the resonant angular frequency of this circuit?
  - What is the average power supplied to the circuit by the generator?
  - What is the average power consumed by the resistor?

#### III

06. On the graphs above and to the right sketch a graph of  $Z$  versus  $\omega$  for a series \_\_\_\_\_ circuit. (Hint: Use a spreadsheet program with the values  $R = 100 \Omega$ ,  $L = 0.250 \text{ H}$ ,  $C = 50.0 \mu\text{F}$ , and  $f$  ranging from 10 Hz to 200 Hz.)
- LR
  - RC
  - LRC



#### Problem 05



**ANSWERS:** 01. a.) 135  $\Omega$    b.) 0.704   c.) 0.157 A   d.) 2.35 W   02. a.) 154  $\Omega$    b.) 0.518   c.) 0.778 A  
 02. d.) 48.4 W   03. a.) 632 rad/s   b.)  $X_L = 31.6 \Omega$ ,  $X_C = 31.6 \Omega$ ,  $Z = 50.0 \Omega$ ,  $I_{\text{rms}} = 1.00 \text{ A}$ ,  $\delta = 0$ ,  $\cos \delta = 1$   
 03. c.)  $X_L = 150 \Omega$ ,  $X_C = 6.67 \Omega$ ,  $Z = 152 \Omega$ ,  $I_{\text{rms}} = 0.329 \text{ A}$ ,  $\delta = 70.8^\circ$ ,  $\cos \delta = 0.329$    04. a.) 2.18-1.45 pF  
 04. b.) 1.54 pF   c.) 2092   06. a.) 0.969 A   b.) 128 V   c.) 24.2 V   d.) 11.0 V   e.) 131 V   f.) 26.6 V  
 06. g.) 330 mJ   h.) 28.2 mJ   i.) 1291 rad/s   j.) 23.5 W   k.) 23.5 W

## Chapter 17

# Engineering Electric Circuits: AC Electric Circuits

## 17.5 LRC Circuits With a Generator/Rectification and Amplification

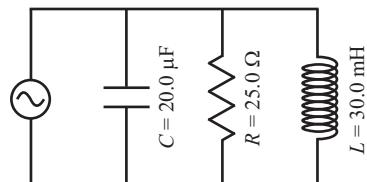
## Homework #149

III

07. In the circuit shown to the right, the variable frequency ac generator produces an rms voltage of 120 V when operated at 60.0 Hz. Assume steady state conditions.

  - Find the rms current that leaves the generator.
  - Find the rms current through the capacitor.
  - Find the rms current through the resistor.
  - Find the rms current through the inductor.
  - What is the phase angle,  $\delta$ ?
  - What is the maximum energy stored in the capacitor?
  - What is the maximum energy stored in the inductor?
  - What is the resonant frequency of this circuit ?
  - What is the minimum rms current for the resonant frequency?

## Problem 07



# Rectification & Amplification

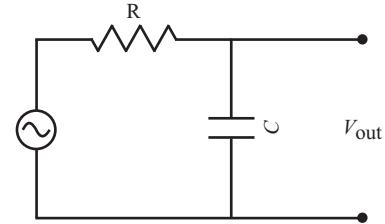
I



9. In the circuit shown to the right, the variable frequency ac generator produces an rms voltage of 120 V, while  $R = 25.0 \Omega$  and  $C = 20 \mu\text{F}$ .

  - What is the capacitive reactance when the frequency is 10.0 Hz?
  - What is the impedance of the circuit when the frequency is 10.0 Hz?
  - What is the rms current when the frequency is 10.0 Hz?
  - What is the output rms voltage when the frequency is 10.0 Hz?
  - What is the capacitive reactance when the frequency is 10,000.0 Hz?
  - What is the impedance of the circuit when the frequency is 10,000.0 Hz?
  - What is the rms current when the frequency is 10,000.0 Hz?
  - What is the output rms voltage when the frequency is 10,000.0 Hz?
  - Why is this called a low-pass filter?

## Problems 09 and 10

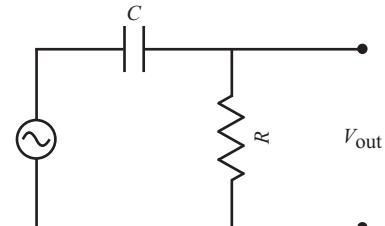


III

10. For the circuit shown above and to the right, write an equation that describes output rms voltage,  $V_{\text{out rms}}$ , as a function of  $V_{\text{in rms}}$ ,  $R$ ,  $C$ , and  $\omega$ .



## Problems 11 and 12



12. For the circuit shown to the right, write an equation that describes output rms voltage,  $V_{\text{out rms}}$ , as a function of  $V_{\text{in rms}}$ ,  $R$ ,  $C$ , and  $\omega$ .

**ANSWERS:** 07. a.) 10.8 A   b.) 0.905 A   c.) 4.80 A   d.) 10.6 A   e.)  $63.7^\circ$    f.) 0.144 J   g.) 1.69 J

**07. h.)** 205 Hz    **i.)** 4.80 A    **08. a.)** 2.12 A    **b.)** 1.06 A

**09. a.)**  $796 \Omega$     **b.)**  $796 \Omega$     **c.)**  $0.151 \text{ A}$     **d.)**  $119.9 \text{ V}$     **e.)**  $0.796 \Omega$     **f.)**  $25.0 \Omega$     **g.)**  $4.80 \text{ A}$     **h.)**  $3.82 \text{ V}$

$$10. V_{\text{out rms}} = \frac{V_{\text{in rms}}}{\sqrt{\alpha^2 C^2 R^2 + 1}}$$

11. a) 376 V b) 1199

$$12. V_{\text{out rms}} = \frac{V_{\text{in rms}}(\omega CR)}{\sqrt{\omega^2 C^2 R^2 + 1}}$$