

## Chapter 13

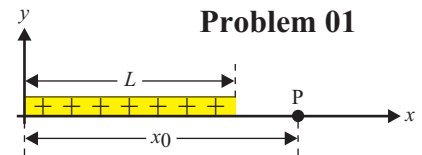
### Engineering Electrostatics: Continuous Charge Distributions

#### 13.1 Electric Field Calculations Using Coulomb's Law Homework # 105

#### II

01. The uniform finite line charge shown in the diagram to the right has a charge of  $Q$  and a length of  $L$ .

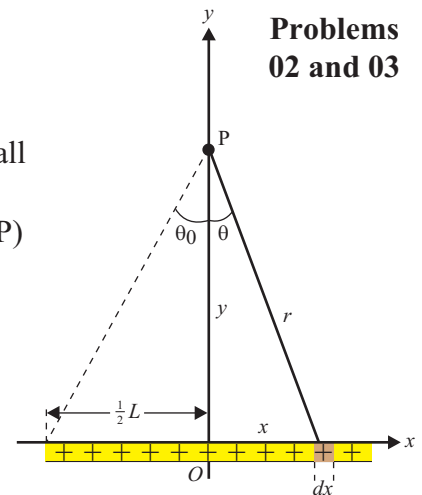
- a.) Determine the linear charge density,  $\lambda$ , for this line charge.
- b.) What is the relationship between a small segment of this line charge,  $dx$ , the small amount of charge in this segment,  $dq$ , and the linear charge density,  $\lambda$ .
- c.) Determine the electric field at point P in terms of  $Q$ ,  $L$ ,  $x_0$ , and Coulomb's constant,  $k$ .
- d.) Determine the electric field at point P in terms of  $Q$ ,  $L$ ,  $x_0$ , and Coulomb's constant,  $k$ , if  $x_0 \gg L$ .
- e.) Determine the electric field at point P with the following data:  $Q = +25.0 \mu\text{C}$ ,  $L = 10.0 \text{ cm}$ , and  $x_0 = 11.4 \text{ cm}$ .
- f.) Determine the electric field at point P with the following data:  $Q = +25.0 \mu\text{C}$ ,  $L = 10.0 \text{ cm}$ , and  $x_0 = 4.65 \text{ m}$ .



**Problem 01**

02. The uniform finite line charge shown in the diagram to the right has a charge of  $Q$  and a length of  $L$ . The  $y$ -axis is a perpendicular bisector of this line charge.

- a.) Determine the linear charge density,  $\lambda$ , for this line charge.
- b.) What is the relationship between a small segment of this line charge,  $dx$ , the small amount of charge in this segment,  $dq$ , and the linear charge density,  $\lambda$ .
- c.) Sketch the vector  $d\vec{E}$  (that represents the electric field from segment  $dx$  at point P) and show its  $x$  and  $y$  components.
- d.) Determine the NET  $x$ -component of the electric field at point P.
- e.) Determine  $\frac{dE_y}{dx}$  at the point P in terms of  $dx$ ,  $r$ ,  $\lambda$ ,  $\theta$ , and Coulomb's constant,  $k$ .
- f.) Determine  $x$  in terms of  $y$  and  $\theta$ .
- g.) Determine  $\frac{dx}{d\theta}$  at the point P in terms of  $r$  and  $y$ .
- h.) Determine  $E_{\text{NET}}$  at point P in terms of  $L$ ,  $y$ ,  $\lambda$ , and Coulomb's constant,  $k$ .
- i.) Determine  $E_{\text{NET}}$  at point P in terms of  $Q$ ,  $y$ , and Coulomb's constant,  $k$ , if  $y \gg L$ .
- j.) Determine  $E_{\text{NET}}$  at point P with the following data:  $Q = +25.0 \mu\text{C}$ ,  $L = 10.0 \text{ cm}$ , and  $y = 6.00 \text{ cm}$ .
- k.) Determine  $E_{\text{NET}}$  at point P with the following data:  $Q = +25.0 \mu\text{C}$ ,  $L = 10.0 \text{ cm}$ , and  $y = 4.65 \text{ m}$ .



**Problems 02 and 03**

03. Assume the uniform line charge shown in the diagram above and to the right is very long (infinite line charge) compared to  $y$ . Determine the electric field at point P in terms of  $y$ ,  $\lambda$ , and Coulomb's constant,  $k$ , if  $L \gg y$ .

ANSWERS: **01.** a.)  $\lambda = \frac{Q}{L}$    b.)  $dq = \lambda \cdot dx$    c.)  $E = k \frac{Q}{x_0(x_0 - L)}$    d.)  $E = k \frac{Q}{x_0^2}$    e.)  $1.48 \times 10^8 \text{ N/C}$

**01.** e.)  $1.04 \times 10^4 \text{ N/C}$    **02.** a.)  $\lambda = \frac{Q}{L}$    b.)  $dq = \lambda \cdot dx$    d.) 0   e.)  $\frac{dE_y}{dx} = k \frac{\lambda dx}{r^2} \cos\theta$  ( $dE_y = k \frac{\lambda dx}{r^2} \cos\theta$ )

**02.** f.)  $x = y \cdot \tan\theta$    g.)  $\frac{dx}{d\theta} = \frac{r^2}{y} (dx = \frac{r^2}{y} d\theta)$    h.)  $E_{\text{NET}} = \frac{k\lambda L}{y\sqrt{(\frac{1}{2}L)^2 + y^2}}$    i.)  $E_{\text{NET}} = k \frac{Q}{y^2}$    j.)  $4.80 \times 10^7 \text{ N/C}$

**02.** k.)  $1.04 \times 10^4 \text{ N/C}$    **03.**  $E_{\text{NET}} = \frac{2k\lambda}{y}$

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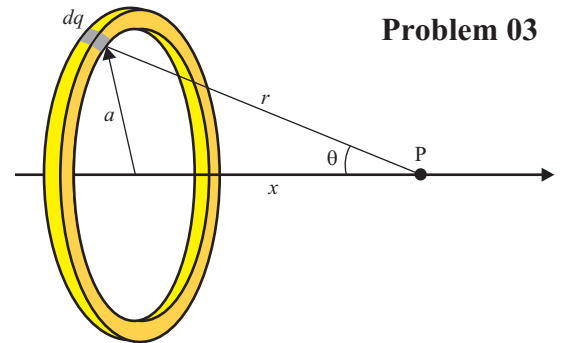
### Engineering Electrostatics: Continuous Charge Distributions

#### 13.1 Electric Field Calculations Using Coulomb's Law Homework # 106

#### II

04. A thin ringed object with a uniform charge of  $Q$  (+) and a radius of  $a$  is shown in the diagram to the right. Notice  $x$ ,  $a$ ,  $\theta$ , and  $r$  are all constants. Point P is on the axis of the ring.

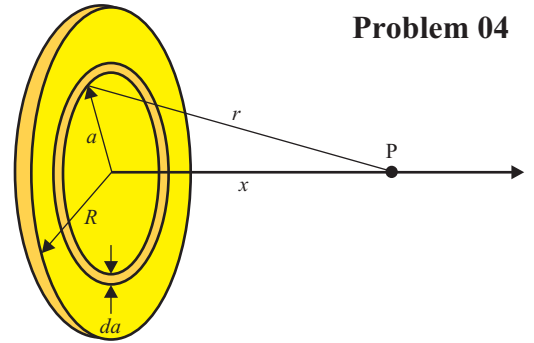
- a.) Sketch the vector  $d\vec{E}$  and show its  $x$  and  $y$  components at point P.
- b.) Determine the **NET**  $y$ -component of the electric field at point P.
- c.) Describe  $dE_x$  in its simplest form in terms of  $x$ ,  $a$ ,  $dq$ , and  $k$ .
- d.) Determine  $E_{\text{NET}}$  at point P in terms of  $Q$ ,  $x$ ,  $a$ , and  $k$ .
- e.) Determine  $E_{\text{NET}}$  at point P in terms of  $Q$ ,  $x$ ,  $a$ , and  $k$ , if  $x \gg a$ .
- f.) Determine  $E_{\text{NET}}$  at point P with the following data:  $Q = +25.0 \mu\text{C}$ ,  $a = 10.0 \text{ cm}$ , and  $x = 6.00 \text{ cm}$ .
- g.) Determine  $E_{\text{NET}}$  at point P with the following data:  $Q = +25.0 \mu\text{C}$ ,  $a = 10.0 \text{ cm}$ , and  $x = 4.65 \text{ m}$ .



**Problem 03**

05. A solid disk with a uniform charge of  $Q$  (+) and a radius of  $R$  is shown in the diagram to the right. Notice  $x$  and  $R$  are both constants. Point P is on the axis of the disk.

- a.) Determine the area charge density,  $\sigma$ , for this disk of charge.
- b.) Sketch the vector  $d\vec{E}$  and show its  $x$  and  $y$  components at point P.
- c.) Determine the **NET**  $y$ -component of the electric field at point P.
- d.) Describe  $dE_x$  in its simplest form in terms of  $x$ ,  $a$ ,  $dq$ , and  $k$ .
- e.) Determine  $E_{\text{NET}}$  at point P in terms of  $Q$ ,  $x$ ,  $a$ , and  $k$ .
- f.) Determine  $E_{\text{NET}}$  at point P in terms of  $Q$ ,  $x$ ,  $a$ , and  $k$ , if  $x \gg R$ .
- g.) Determine  $E_{\text{NET}}$  at point P in terms of  $Q$ ,  $x$ ,  $a$ , and  $k$ , if  $R \gg x$  (as if the disk were an infinite plane of charge).
- h.) Determine  $E_{\text{NET}}$  at point P with the following data:  $Q = +25.0 \mu\text{C}$ ,  $R = 10.0 \text{ cm}$ , and  $x = 6.00 \text{ cm}$ .
- i.) Determine  $E_{\text{NET}}$  at point P with the following data:  $Q = +25.0 \mu\text{C}$ ,  $R = 10.0 \text{ cm}$ , and  $x = 4.65 \text{ m}$ .
- j.) Determine  $E_{\text{NET}}$  at point P with the following data:  $Q = +25.0 \mu\text{C}$ ,  $R = 4.65 \text{ m}$ , and  $x = 6.00 \text{ cm}$ .



**Problem 04**

ANSWERS: 04. b.) 0    c.)  $dE_x = k \frac{dq}{(x^2 + a^2)^{3/2}} x$     d.)  $E_{\text{NET}} = \frac{kQx}{(x^2 + a^2)^{3/2}}$     e.)  $E_{\text{NET}} = k \frac{Q}{x^2}$     f.)  $8.51 \times 10^6 \text{ N/C}$

04. f.)  $1.04 \times 10^4 \text{ N/C}$     05. a.)  $\sigma = \frac{Q}{A} = \frac{Q}{\pi R^2}$     c.) 0    d.)  $dE_x = \pi k \sigma \frac{2ada}{(x^2 + a^2)^{3/2}} x$     e.)  $E_{\text{NET}} = 2\pi k \sigma \left(1 - \frac{x}{\sqrt{x^2 + R^2}}\right)$

05. f.)  $E_{\text{NET}} = k \frac{Q}{x^2}$     g.)  $E_{\text{NET}} = 2\pi k \sigma = \frac{\sigma}{2\epsilon_0}$     h.)  $2.18 \times 10^7 \text{ N/C}$     i.)  $1.04 \times 10^4 \text{ N/C}$     j.)  $2.08 \times 10^4 \text{ N/C}$

# Chapter 13

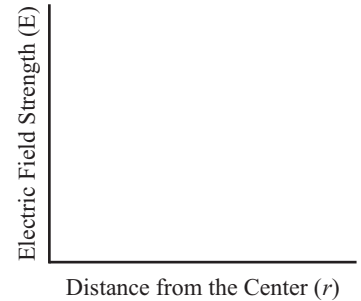
## Engineering Electrostatics: Continuous Charge Distributions

### 13.2 Electric Field Calculations Using Gauss's Law Homework # 107

#### II

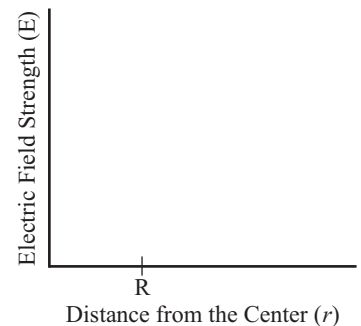
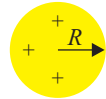
01. A point charge with a charge of  $Q$  (+) is shown in the diagram to the right.
- Sketch the electric field lines on the diagram to the right.
  - What should be the shape of a Gaussian surface such that the strength of the electric field will be a constant everywhere on this surface and the direction of the electric field will be perpendicular to the surface at all points on the surface?
  - Use Gauss's law to derive a mathematical expression to predict the electric field strength as a function of its distance,  $r$ , from the point source.
  - On the graph to the right and below, graph the expression derived in c.) above.
02. If the point charge in the diagram above and to the right has a charge of  $+25.0 \mu\text{C}$ , find the field strength at a distance of 6.00 cm from the point source.

**Problems 01 and 02**



03. A hollow spherical shell (negligible thickness) with a uniformly distributed charge is shown in the diagram to the right. The shell has a net charge of  $Q$  (+) and a radius of  $R$ .
- Sketch the electric field lines on the diagram to the right.
  - What is the surface charge density,  $\sigma$ , of the spherical shell?
  - What should be the shape of a Gaussian surface such that the strength of the electric field will be a constant everywhere on this surface and the direction of the electric field will be perpendicular to the surface at all points on the surface?
  - Use Gauss's law predict the electric field anywhere inside the shell.
  - Use Gauss's law to derive a mathematical expression to predict the electric field strength as a function of its distance outside the spherical shell.
  - On the graph to the right and below, graph the expression derived in d.) and e.) above.
  - What is the difference in electric field strength between a point just inside the spherical shell and one just outside (the amount of discontinuity).

**Problems 03 and 04**



04. Assume the shell in the diagram above and to the right has a charge of  $+25.0 \mu\text{C}$  and a radius of 10.0 cm.
- What is the surface charge density,  $\sigma$ , of the spherical shell?
  - Find the field strength at a distance of 6.00 cm from the center of the shell.
  - Find the field strength at a distance of 16.00 cm from the center of the shell.
  - Find the field strength at a distance of 6.00 m from the center of the shell.

**ANSWERS:** 01. b.) sphere    c.)  $E_{\text{NET}} = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2}$     02.  $6.25 \times 10^7 \text{ N/C}$

03. b.)  $\sigma = \frac{Q}{A} = \frac{Q}{4\pi R^2}$     c.) sphere    d.) 0    e.)  $E_{\text{NET}} = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2} = \frac{\sigma}{\epsilon_0}$     g.)  $\frac{\sigma}{\epsilon_0}$

04. a.)  $199 \mu\text{C/m}^2$     b.) 0    c.)  $8.79 \times 10^6 \text{ N/C}$     d.)  $6250 \text{ N/C}$

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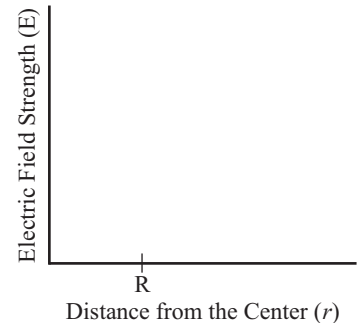
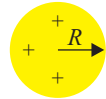
## Engineering Electrostatics: Continuous Charge Distributions

### 13.2 Electric Field Calculations Using Gauss's Law Homework # 108

#### II

05. A solid spherical insulating material with a uniformly distributed charge is shown in the diagram to the right. The sphere has a net charge of  $Q$  (+) and a radius of  $R$ .
- Sketch the electric field lines on the diagram to the right.
  - What is the charge density,  $\rho$ , of the sphere?
  - What should be the shape of a Gaussian surface such that the strength of the electric field will be a constant everywhere on this surface and the direction of the electric field will be perpendicular to the surface at all points on the surface?
  - Use Gauss's law predict the electric field anywhere inside the sphere.
  - Use Gauss's law to derive a mathematical expression to predict the electric field strength as a function of its distance outside the sphere.
  - On the graph to the right and below, graph the expression derived in d.) and e.) above.
  - What is the difference in electric field strength between a point just inside the sphere and one just outside the sphere (the amount of discontinuity).

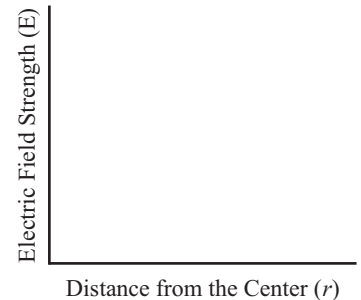
#### Problems 05 & 06



06. Assume the solid sphere in the diagram above and to the right has a charge of  $+25.0 \mu\text{C}$  and a radius of  $10.0 \text{ cm}$ .
- What is the charge density,  $\rho$ , of the sphere?
  - Find the field strength at a distance of  $6.00 \text{ cm}$  from the center of the sphere.
  - Find the field strength at a distance of  $16.00 \text{ cm}$  from the center of the sphere.
  - Find the field strength at a distance of  $6.00 \text{ m}$  from the center of the sphere.

#### Problems 07 and 08

07. An infinite line charge with a uniformly distributed charge shown in the diagram to the right has a linear charge density of  $\lambda$ .
- Sketch the electric field lines on the diagram to the right.
  - What should be the shape of a Gaussian surface such that the strength of the electric field will be a constant everywhere on this surface and the direction of the electric field will be perpendicular to the surface at all points on the surface?
  - Use Gauss's law to derive a mathematical expression to predict the electric field strength as a function of its distance from the line charge.
  - On the graph to the right and below, graph the expression derived in c.) above.



08. Assume the infinite line charge in the diagram above and to the right has a line charge density,  $\lambda$ , of  $+250 \mu\text{C}/\text{m}$ .
- Find the field strength at a distance of  $6.00 \text{ cm}$  from the line charge.
  - Find the field strength at a distance of  $16.00 \text{ cm}$  from the line charge.
  - Find the field strength at a distance of  $6.00 \text{ m}$  from the line charge.

ANSWERS: 05. b.)  $\rho = \frac{Q}{V} = \frac{Q}{\frac{4}{3}\pi R^3}$  c.) sphere d.)  $E_{\text{NET}} = \frac{\rho}{3\epsilon_0} r = \frac{1}{4\pi\epsilon_0} \frac{Q}{R^3} r = k \frac{Q}{R^3} r$  e.)  $E_{\text{NET}} = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2} = k \frac{Q}{r^2}$   
 05. g.) no discontinuity (continuous) 06. a.)  $5.97 \text{ mC}/\text{m}^3$  b.)  $1.37 \times 10^7 \text{ N}/\text{C}$  c.)  $8.79 \times 10^6 \text{ N}/\text{C}$  d.)  $6250 \text{ N}/\text{C}$   
 07. b.) cylinder c.)  $E_{\text{NET}} = \frac{1}{2\pi\epsilon_0} \frac{\lambda}{r} = \frac{2k\lambda}{r}$  08. a.)  $7.50 \times 10^7 \text{ N}/\text{C}$  b.)  $2.81 \times 10^7 \text{ N}/\text{C}$  c.)  $7.50 \times 10^5 \text{ N}/\text{C}$

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### Engineering Electrostatics: Continuous Charge Distributions

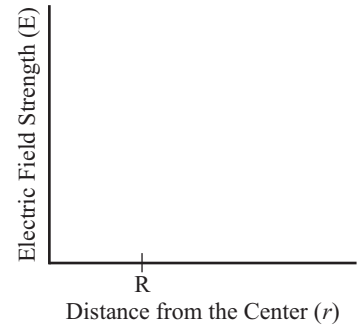
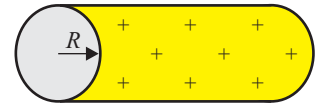
#### 13.2 Electric Field Calculations Using Gauss's Law Homework # 109

#### II

09. A hollow cylindrical shell (negligible thickness) with a uniformly distributed charge is shown in the diagram to the right. The shell has a net charge of  $Q$  (+), a radius of  $R$ , and a length of  $L$ .

#### Problems 09 and 10

- a.) Sketch the electric field lines on the diagram to the right.
- b.) What is the surface charge density,  $\sigma$ , of the cylindrical shell?
- c.) What should be the shape of a Gaussian surface such that the strength of the electric field will be a constant everywhere on this surface and the direction of the electric field will be perpendicular to the surface at all points on the surface?
- d.) Use Gauss's law predict the electric field anywhere inside the shell.
- e.) Use Gauss's law to derive a mathematical expression to predict the electric field strength as a function of its distance outside the cylindrical shell.
- f.) On the graph to the right, graph the expression derived in d.) and e.) above.
- g.) What is the difference in electric field strength between a point just inside the cylindrical shell and one just outside (the amount of discontinuity).

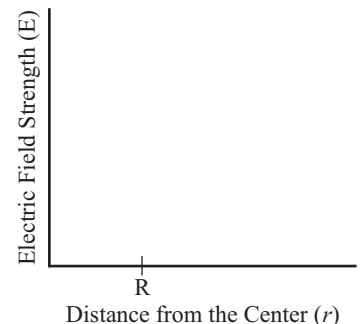
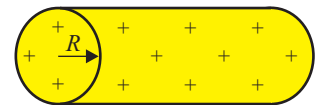


10. Assume the shell in the diagram above and to the right has a charge of  $+25.0 \mu\text{C}$ , a radius of  $10.0 \text{ cm}$ , and a length of  $20.0 \text{ cm}$ .

- a.) What is the surface charge density,  $\sigma$ , of the spherical shell?
- b.) Find the field strength at a distance of  $6.00 \text{ cm}$  from the center of the shell.
- c.) Find the field strength at a distance of  $16.00 \text{ cm}$  from the center of the shell.
- d.) Find the field strength at a distance of  $6.00 \text{ m}$  from the center of the shell.

11. An infinitely long solid cylindrical insulating material with a uniformly distributed charge is shown in the diagram to the right. The cylinder has a net charge of  $Q$  (+) and a radius of  $R$ .

#### Problem 11



- a.) What is the charge density,  $\rho$ , of the cylinder?
- b.) What should be the shape of a Gaussian surface such that the strength of the electric field will be a constant everywhere on this surface and the direction of the electric field will be perpendicular to the surface at all points on the surface?
- c.) Use Gauss's law predict the electric field anywhere inside the cylinder.
- d.) Use Gauss's law to derive a mathematical expression to predict the electric field strength as a function of its distance outside the cylinder.
- e.) On the graph to the right, graph the expression derived in c.) and d.) above.
- f.) What is the difference in electric field strength between a point just inside the cylinder and one just outside the sphere (the amount of discontinuity).

12. Consider an infinite plane of charge with a surface charge density of  $\sigma$ .

- a.) What is the **NET** electric field near the plane.
- b.) What is the amount of discontinuity of the electric fields on the two sides of the plane?

ANSWERS: **09.** b.)  $\sigma = \frac{Q}{A} = \frac{Q}{2\pi RL}$  c.) cylinder d.) 0 e.)  $E_{\text{NET}} = \frac{1}{2\pi\epsilon_0} \frac{\lambda}{r} = \frac{2k\lambda}{r}$  g.)  $\frac{\sigma}{\epsilon_0}$  **10.** a.)  $199 \mu\text{C}/\text{m}^2$   
**10.** b.) 0 c.)  $1.40 \times 10^7 \text{ N/C}$  d.)  $3.75 \times 10^5 \text{ N/C}$  **11.** a.)  $\rho = \frac{Q}{V} = \frac{Q}{\pi R^2 L}$  b.) cylinder  
**11.** c.)  $E_{\text{NET}} = \frac{\rho}{2\epsilon_0} r = \frac{\lambda}{2\pi\epsilon_0 R^2} r$  d.)  $E_{\text{NET}} = \frac{1}{2\pi\epsilon_0} \frac{\lambda}{r}$  f.) no discontinuity (continuous) **12.** a.)  $E_{\text{NET}} = \frac{\sigma}{2\epsilon_0}$  b.)  $\frac{\sigma}{\epsilon_0}$

# Chapter 13

## Engineering Electrostatics: Continuous Charge Distributions

### 13.3 Potential Calculations of Continuous Charge Distributions      Homework # 110

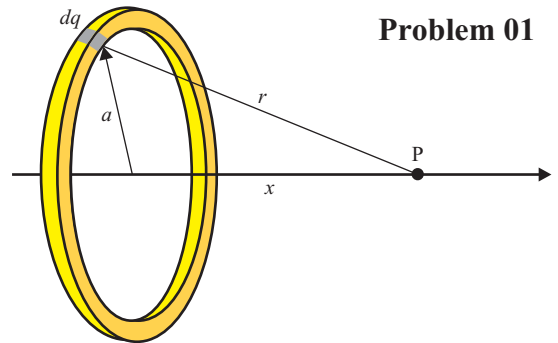
#### II

01. A thin ringed object with a uniform charge of  $Q$  (+) and a radius of  $a$  is shown in the diagram to the right. Notice  $x$ ,  $a$ , and  $r$  are all constants. Point P is on the axis of the ring.

- a.) What is the potential at point P?
- b.) How much work would be required to move a positive charge of  $q$  from point P to a very large distance away (infinity)?

**For parts c.) and d.) assume  $Q = +25.0 \mu\text{C}$ ,  $a = 10.0 \text{ cm}$ , and  $x = 6.00 \text{ cm}$ .**

- c.) Determine the potential at point P.
- d.) How much work would be required to move a proton from point P to a very large distance away (infinity)?



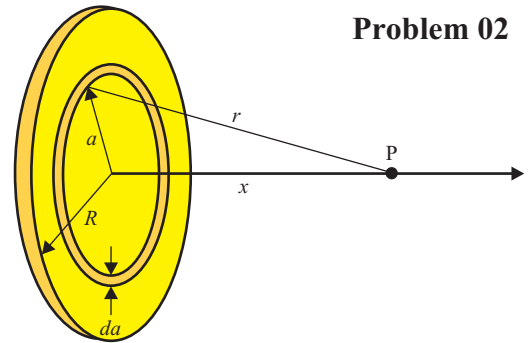
**Problem 01**

02. A solid disk with a uniform charge of  $Q$  (+) and a radius of  $R$  is shown in the diagram to the right. Notice  $x$  and  $R$  are both constants. Point P is on the axis of the disk.

- a.) What is the potential at point P?
- b.) How much work would be required to move a positive charge of  $q$  from point P to a very large distance away (infinity)?

**For parts c.) and d.) assume  $Q = +25.0 \mu\text{C}$ ,  $R = 10.0 \text{ cm}$ , and  $x = 6.00 \text{ cm}$ .**

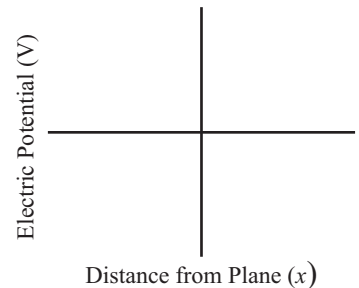
- c.) Determine the potential at point P.
- d.) How much work would be required to move a proton from point P to a very large distance away (infinity)?



**Problem 02**

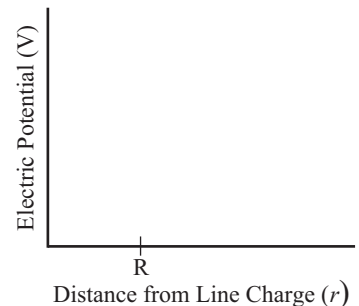
03. Consider an infinite vertical plane of charge oriented along the  $y$ -axis with a surface charge density of  $\sigma$ .

- a.) Write a mathematical expression that describes the potential as a function of distance from the plane along the  $x$ -axis (both positive and negative  $x$ -axis). Assume the potential at the vertical plane of charge ( $x = 0$ ) is 100 V.
- b.) Sketch a graph of the expression determined in a.) above. Is the graph continuous?



04. A hollow spherical shell (negligible thickness) with a uniformly distributed charge has a net charge of  $Q$  (+) and a radius of  $R$ .

- a.) Write a mathematical expression that describes the potential as a function of distance from the center of the shell,  $r$  (both inside and outside the shell).
- b.) Sketch a graph of the expression determined in a.) above. Is the graph continuous?



05. Consider an infinite line charge with a uniformly distributed charge that has a linear charge density of  $\lambda$ . Write a mathematical expression that describes the potential as a function of distance from the line charge,  $r$ . Assume  $V = 100 \text{ V}$  at  $r = 10.0 \text{ cm}$ .

**ANSWERS:** 01. a.)  $V = k \frac{Q}{\sqrt{x^2 + a^2}}$     b.)  $W_{P\infty} = k \frac{Qq}{\sqrt{x^2 + a^2}}$     c.)  $1.93 \times 10^6 \text{ V}$     d.)  $3.09 \times 10^{-13} \text{ J}$

02. a.)  $V = 2\pi k\sigma(\sqrt{x^2 + R^2} - x)$     b.)  $W_{P\infty} = 2\pi k\sigma(\sqrt{x^2 + R^2} - x)q$     c.)  $2.55 \times 10^6 \text{ V}$     d.)  $4.08 \times 10^{-13} \text{ J}$

03. a.)  $V(x) = 100 - \frac{\sigma}{2\epsilon_0}x$     b.) yes    04. a.)  $V(r) = k\frac{Q}{R}$  ( $r \leq R$ ),  $V(r) = k\frac{Q}{r}$  ( $r > R$ )    b.) yes

05.  $V(r) = 100 - 2k\lambda \ln\left(\frac{r}{0.10}\right)$

## Chapter 13

### Engineering Electrostatics: Continuous Charge Distributions

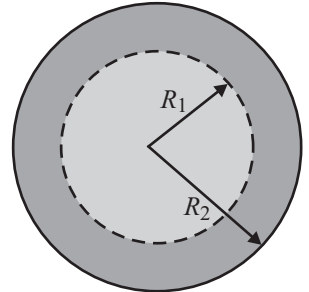
#### 13.4 Electric Field and Potential of Multiple Charged Objects

#### Homework # 111

#### II

01. The diagram to the right shows the cross section of two concentric, conducting spherical shells (each with negligible thickness). The smaller, inner shell has a radius,  $R_1$ , of 6.00 cm and a charge,  $Q_1$ , of  $+18.0 \mu\text{C}$ . The larger, outer shell has a radius,  $R_2$ , of 9.00 cm and a charge,  $Q_2$ , of  $-11.0 \mu\text{C}$ .

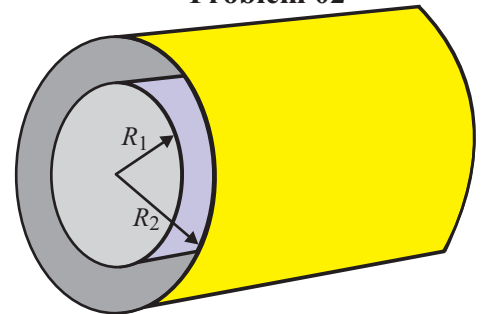
#### Problem 01



- a.) Write an equation describing the **NET** electric field inside the inner shell (where  $r \leq R_1$ ).
- b.) Write an equation describing the **NET** electric field as a function of distance from the center,  $r$ , for  $R_1 < r \leq R_2$ .
- c.) Write an equation describing the **NET** electric field as a function of distance from the center,  $r$ , where  $r > R_2$ .
- d.) What is the **NET** electric field 4.00 cm outside the outer shell?
- e.) What is the **NET** electrostatic potential of the outer shell?
- f.) Determine the constant of integration when calculating the **NET** electrostatic potential between the two shells.
- g.) What is the **NET** electrostatic potential of the inner shell?
- h.) What is the potential difference between the inner shell and the outer shell?
- i.) What is the **NET** electrostatic potential at the center of the two shells?
- j.) How much work would be required to move an electron from the inner shell to the outer shell?
- k.) How much work would be required to move a proton from infinity to the outer shell?

02. The diagram to the right shows two concentric, conducting cylindrical shells (each with negligible thickness). The radii ( $R_1 = 6.00 \text{ cm}$  and  $R_2 = 9.00 \text{ cm}$ ) and charges ( $Q_1 = +18.0 \mu\text{C}$  and  $Q_2 = -11.0 \mu\text{C}$ ) of these cylindrical shells are identical to those of the spherical shells in problem 01 above. Both shells have an equal length of 60.0 cm. Assume the **NET** electrostatic potential is zero at a radial distance of 100.0 m from the center of the two shells.

#### Problem 02



- a.) Write an equation describing the **NET** electric field inside the inner shell (where  $r \leq R_1$ ).
- b.) Write an equation describing the **NET** electric field as a function of distance from the center,  $r$ , for  $R_1 < r \leq R_2$ .
- c.) Write an equation describing the **NET** electric field as a function of distance from the center,  $r$ , where  $r > R_2$ .
- d.) What is the **NET** electric field 4.00 cm outside the outer shell?
- e.) Determine the constant of integration when calculating the **NET** electrostatic potential outside the two shells.
- f.) What is the **NET** electrostatic potential of the outer shell?
- g.) Determine the constant of integration when calculating the **NET** electrostatic potential between the two shells.
- h.) What is the **NET** electrostatic potential of the inner shell?
- i.) What is the potential difference between the inner shell and the outer shell?
- j.) What is the **NET** electrostatic potential at the center of the two shells?
- k.) How much work would be required to move an electron from the inner shell to the outer shell?
- l.) How much work would be required to move a proton from a position 100.0 m from the center to the outer shell?

ANSWERS: 01. a.)  $E = 0$    b.)  $E = \frac{1}{4\pi\epsilon_0} \frac{Q_1}{r^2} = \frac{1.62 \times 10^5}{r^2}$    c.)  $E = \frac{1}{4\pi\epsilon_0} \frac{(Q_1 + Q_2)}{r^2} = \frac{6.30 \times 10^4}{r^2}$    d.)  $3.73 \times 10^6 \text{ N/C}$   
 01. e.)  $7.00 \times 10^5 \text{ V}$    f.)  $-1.10 \times 10^6 \text{ V}$    g.)  $1.60 \times 10^6 \text{ V}$    h.)  $9.00 \times 10^5 \text{ V}$    i.)  $1.60 \times 10^6 \text{ V}$    j.)  $1.44 \times 10^{-13} \text{ J}$   
 01. k.)  $1.12 \times 10^{-13} \text{ J}$    02. a.)  $E = 0$    b.)  $E = \frac{1}{2\pi\epsilon_0} \frac{\lambda_1}{r} = 2k \frac{Q_1/L}{r} = \frac{5.40 \times 10^5}{r}$    c.)  $E = \frac{1}{2\pi\epsilon_0} \frac{\lambda_1 + \lambda_2}{r} = 2k \frac{(Q_1 + Q_2)/L}{r} = \frac{2.10 \times 10^5}{r}$   
 02. d.)  $1.62 \times 10^6 \text{ N/C}$    e.)  $9.67 \times 10^5 \text{ V}$    f.)  $1.47 \times 10^6 \text{ V}$    g.)  $1.72 \times 10^5 \text{ V}$    h.)  $1.69 \times 10^6 \text{ V}$    i.)  $2.19 \times 10^5 \text{ V}$   
 02. j.)  $1.69 \times 10^6 \text{ V}$    k.)  $3.50 \times 10^{-14} \text{ J}$    l.)  $2.36 \times 10^{-13} \text{ J}$

## Chapter 13

### Engineering Electrostatics: Continuous Charge Distributions

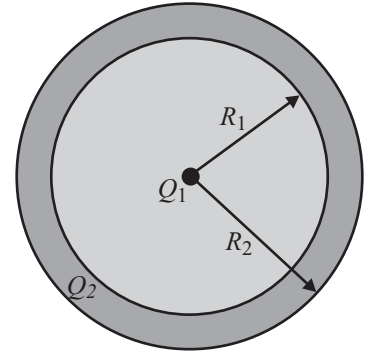
#### 13.4 Electric Field and Potential of Multiple Charged Objects

#### Homework # 112

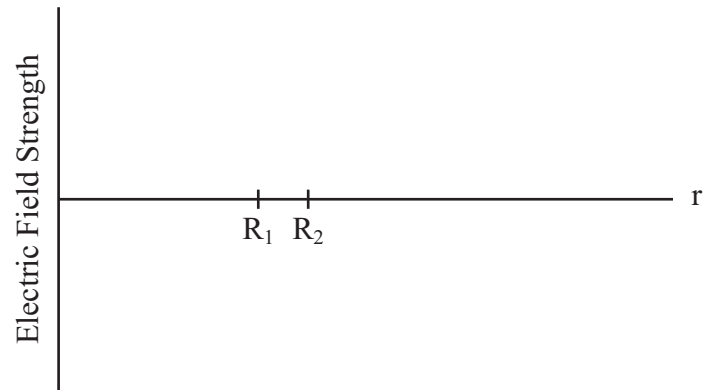
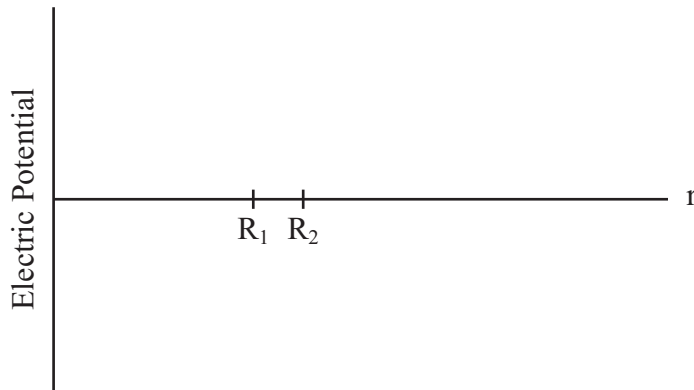
#### II

03. The diagram to the right shows the cross section of a conducting spherical shell with a thickness of 2.00 cm. The inner surface of the shell has a radius,  $R_1$ , of 8.00 cm, while the outer surface has a radius,  $R_2$ , of 10.00 cm. The charge on the shell is  $Q_2 = +14.00 \mu\text{C}$ . The shell encloses a point charge located at its center with a charge of  $Q_1 = -5.00 \mu\text{C}$ .

#### Problem 03



- a.) What is the **NET** electrostatic potential just outside the shell?
- b.) What is the **NET** electrostatic potential just inside the shell?
- c.) What is the **NET** electrostatic potential at the center of the shell (at  $Q_1$ )?
- d.) Determine the constant of integration when calculating the **NET** electrostatic potential inside the inner the wall of the shell.
- e.) What is the **NET** electrostatic potential 3.00 cm from the central charge?
- f.) Where, other than infinity, will the **NET** electrostatic potential be zero?
- g.) On the graph below, sketch the electric potential as a function of distance,  $r$ , from  $Q_1$ .
- h.) On the graph below and to the right, sketch the electric field strength as a function of distance,  $r$ , from  $Q_1$ .



ANSWERS: **03.** a.)  $8.10 \times 10^5 \text{ V}$    b.)  $8.10 \times 10^5 \text{ V}$    c.)  $\infty$    d.)  $1.3725 \times 10^6 \text{ V}$    e.)  $-1.275 \times 10^5 \text{ V}$   
**03.** f.) 3.28 cm from  $Q_1$



# Chapter 13

## Engineering Electrostatics: Continuous Charge Distributions

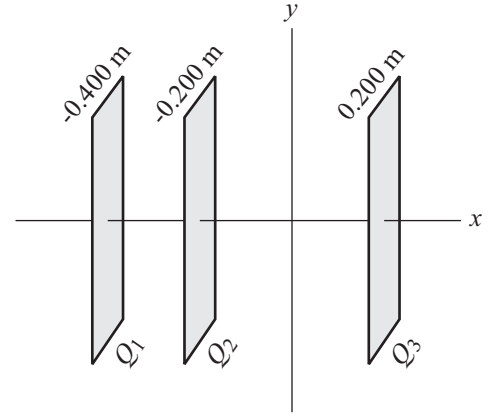
### 13.4 Electric Field and Potential of Multiple Charged Objects

### Homework # 113

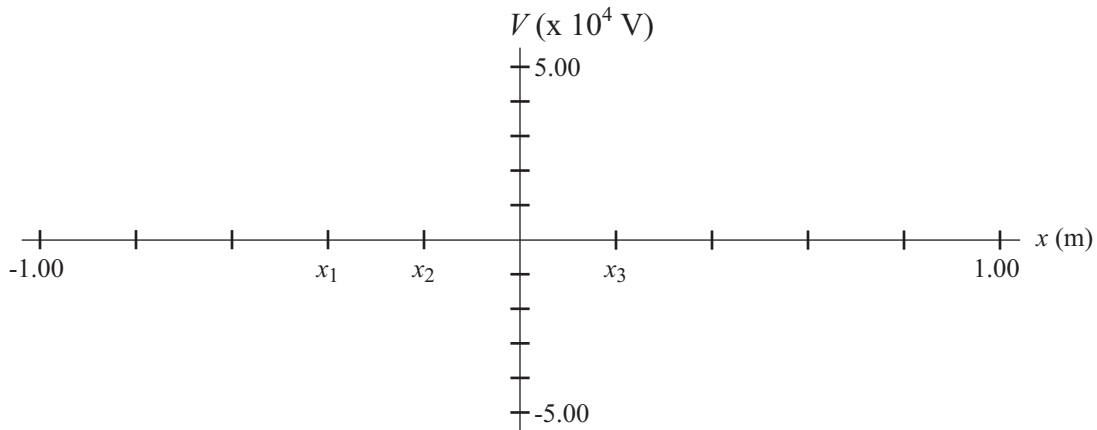
#### III

04. Each of the three vertical, parallel, conducting plates shown in the diagram to the right has an area of  $2.00 \text{ m}^2$ . The first plate contains a charge of  $Q_1 = +8.00 \text{ } \mu\text{C}$  and is located at  $x_1 = -0.400 \text{ m}$ . The second plate contains a charge of  $Q_2 = -8.00 \text{ } \mu\text{C}$  and is located at  $x_2 = -0.200 \text{ m}$ . The third plate contains a charge of  $Q_3 = +4.00 \text{ } \mu\text{C}$  and is located at  $x_3 = 0.200 \text{ m}$ . Assume the **NET** electric potential is zero at the origin.

#### Problem 04



- a.) Determine the **NET** electric field to the left of plate 1.
- b.) Determine the **NET** electric field between plates 1 and 2.
- c.) Determine the **NET** electric field between plates 2 and 3.
- d.) Determine the **NET** electric field to the right of plate 3.
- e.) Determine the **NET** electric potential of each plate ( $V_1, V_2,$  and  $V_3$ ).
- f.) Where, other than the origin, is the **NET** electric potential zero?
- g.) On the graph below, sketch the potential as a function of position along the  $x$ -axis.
- h.) What is the potential difference between plates 1 and 2?
- i.) How much work would be required to move an electron from plate 3 to plate 1?



ANSWERS: **04.** a.)  $-1.13 \times 10^5 \text{ N/C}$     b.)  $3.39 \times 10^5 \text{ N/C}$     c.)  $-1.13 \times 10^5 \text{ N/C}$     d.)  $1.13 \times 10^5 \text{ N/C}$   
**04.** e.)  $V_1 = 4.52 \times 10^4 \text{ V}, V_2 = -2.26 \times 10^4 \text{ V}, V_3 = 2.26 \times 10^4 \text{ V}$     f.)  $x = -0.800 \text{ m}, -0.267 \text{ m}, 0.400 \text{ m}$   
**04.** h.)  $6.78 \times 10^4 \text{ V}$     i.)  $3.62 \times 10^{-15} \text{ J}$